# Nonparametric Estimation of the Potential Impact Fraction and the Population Attributable Fraction

#### Colleen Chan

#### Yale University, Dept. of Statistics and Data Science

Collaborators: Rodrigo Zepeda-Tello<sup>1</sup>, Dalia Camacho García Formentí<sup>1</sup>, Frederick Cudhea<sup>2</sup>, Rafael Meza<sup>3</sup>, Eliane Rodrigues<sup>4</sup>, Tonatiuh Barrientos Gutierrez<sup>1</sup>, Donna Spiegelman<sup>5</sup>, Xin Zhou<sup>5</sup>

<sup>1</sup>National Institute of Public Health of Mexico, <sup>2</sup>Tufts University Friedman School of Nutrition Science and Policy, <sup>3</sup>University of Michigan School of Public Health, <sup>4</sup>Universidad Nacional Autonoma de Mexico, <sup>5</sup>Yale School of Public Health

Paper link: https://arxiv.org/abs/2207.03597

#### IBC 2022 Young Statistician's Showcase

12 July, 2022

# SSB's and Type 2 Diabetes

Sugar-sweetened beverages (SSB's)

- Drinks with added sugar
- The largest source of added sugar in our diets today. SSB intake has risen most dramatically in LMIC's<sup>1</sup>
- SSB consumption linked to increased risk of T2D, obesity, heart disease



<sup>&</sup>lt;sup>1</sup>Malik et al., *Nature Reviews Endocrinology*, 2022.

# SSB's and Type 2 Diabetes

Sugar-sweetened beverages (SSB's)

- Drinks with added sugar
- The largest source of added sugar in our diets today. SSB intake has risen most dramatically in LMIC's<sup>1</sup>
- SSB consumption linked to increased risk of T2D, obesity, heart disease



**Q:** What fraction of type 2 diabetes cases can be attributed to SSB consumption? What if SSB consumption were entirely eliminated? What if it were halved?

<sup>&</sup>lt;sup>1</sup>Malik et al., *Nature Reviews Endocrinology*, 2022.

### The PIF and PAF

- The potential impact fraction (PIF), or the attributable fraction, is the proportion of incidents attributable to a given risk factor
- It requires a relative risk (RR) function that depends on exposure levels X and regression coefficients  $\beta$ 
  - Most common form  $RR(\boldsymbol{X}; \boldsymbol{\beta}) = \exp(\boldsymbol{X}\boldsymbol{\beta})$

### The PIF and PAF

- The potential impact fraction (PIF), or the attributable fraction, is the proportion of incidents attributable to a given risk factor
- It requires a relative risk (RR) function that depends on exposure levels **X** and regression coefficients  $\beta$ 
  - Most common form  $RR(\boldsymbol{X}; \boldsymbol{\beta}) = \exp(\boldsymbol{X}\boldsymbol{\beta})$

#### Definition

The potential impact fraction (PIF) is defined as

$$\mathsf{PIF} = \frac{\mathbb{E}_{\boldsymbol{X}}^{\mathrm{obs}} \left[ \mathsf{RR}(\boldsymbol{X}; \boldsymbol{\beta}) \right] - \mathbb{E}_{\boldsymbol{X}}^{\mathrm{cft}} \left[ \mathsf{RR}(\boldsymbol{X}; \boldsymbol{\beta}) \right]}{\mathbb{E}_{\boldsymbol{X}}^{\mathrm{obs}} \left[ \mathsf{RR}(\boldsymbol{X}; \boldsymbol{\beta}) \right]},$$
(1)

where  $\mathbb{E}_{\mathbf{X}}^{\text{obs}}[RR(\mathbf{X};\beta)]$  represents the expected value of the relative risk under the observed exposure distribution and  $\mathbb{E}_{\mathbf{X}}^{\text{cft}}[RR(\mathbf{X};\beta)]$  is the expected value of the relative risk under a counterfactual distribution of the exposure.

### The PIF and PAF

The population attributable fraction (PAF), or the attributable fraction for the population, is a specific case of the PIF when the counterfactual exposure is 0 (E<sup>cft</sup><sub>X</sub> [RR(X; β)] = 1)

#### Definition

The population attributable fraction (PAF) is defined as

$$\mathsf{PAF} = 1 - rac{1}{\mathbb{E}^{\mathrm{obs}}_{oldsymbol{X}}\left[\mathsf{RR}(oldsymbol{X};oldsymbol{eta})
ight]},$$

where  $\mathbb{E}_{\mathbf{X}}^{\text{obs}}[RR(\mathbf{X};\beta)]$  represents the expected value of the relative risk under the observed exposure distribution in a given population.

(2)

# Standard Approach<sup>1</sup>

- Assume a parametric distribution for continuous exposure X (e.g. Log normal, Weibull, Gamma)
- 2 Fit the parameters using method of moments estimation, matching the mean and variance of the observed exposure data
- **3** Estimate the PIF from Eq. 1 or the PAF from Eq. 2 using analytic or numerical integration

<sup>&</sup>lt;sup>1</sup>GBD 2013 Risk Factors et al., 2015, Gortmaker et al., 2016, Veerman et al., 2016

# Standard Approach<sup>1</sup>

- Assume a parametric distribution for continuous exposure X (e.g. Log normal, Weibull, Gamma)
- 2 Fit the parameters using method of moments estimation, matching the mean and variance of the observed exposure data
- **3** Estimate the PIF from Eq. 1 or the PAF from Eq. 2 using analytic or numerical integration

Issues with the standard approach:

- **1** PIF is undefined for heavy-tailed exposure distributions
- 2 PIF can be heavily biased if exposure distribution is misspecified

<sup>1</sup>GBD 2013 Risk Factors et al., 2015, Gortmaker et al., 2016, Veerman et al., 2016

### **Undefined PIF's?**

$$\mathsf{PAF} = 1 - rac{1}{\mathbb{E}^{\mathrm{obs}}_{oldsymbol{X}}\left[\mathsf{RR}oldsymbol{(oldsymbol{X};oldsymbol{eta})}
ight]}$$

- The problem lies on the combination of a heavy-tailed distribution with an exponential relative risk
- A random variable X is said to have a heavy tail if the tail probabilities P(X > t) decay more slowly than tails of any exponential distribution

$$\lim_{x\to\infty}e^{cx}P(X>x)=\infty \text{ for all positive } c$$

• Distributions with heavy tails: Log normal, Pareto, Cauchy, Weibull with shape parameter less than 1

# **Standard Approach**

**Table:** Relative bias percentage of PAF under different distributional assumptions for the standard method.

		Distribution assumed			
True distribution	True PAF	Gamma	Log normal	Normal	Weibull
Gamma(1.15, 1.29)	0.3455				
Normal(1.48, 1.38)	0.3795				
Weibull(1.08, 1.53)	0.3447				

# **Standard Approach**

**Table:** Relative bias percentage of PAF under different distributional assumptions for the standard method.

		Distribution assumed			
True distribution	True PAF	Gamma	Log normal	Normal	Weibull
Gamma(1.15, 1.29)	0.3455	0			
Normal(1.48, 1.38)	0.3795			0	
Weibull(1.08, 1.53)	0.3447				0

# **Standard Approach**

**Table:** Relative bias percentage of PAF under different distributional assumptions for the standard method.

		Distribution assumed			
True distribution	True PAF	Gamma	Log normal	Normal	Weibull
Gamma(1.15, 1.29)	0.3455	0	189.4	-19.6	-0.2
Normal(1.48, 1.38)	0.3795	-9.2	163.5	0	-9.3
Weibull (1.08, 1.53)	0.3447	0.2	190.1	-19.2	0

# (Kehoe) Mixture Approach

To avoid undefined PIF values, Kehoe et al. (2012) proposes:

- Truncate the assumed exposure distribution by an upper bound M
- Fit the exposure data using maximum likelihood estimation. Separate out 0 and positive values of the exposure

$$\mathsf{PAF} = 1 - rac{1}{p_0 R R_0 + \int_0^M R R(\boldsymbol{X}; \boldsymbol{\beta}) f(\boldsymbol{X}) \mathsf{d} \boldsymbol{X}}$$

### **Mixture Approach**

PIF value now depends on truncation bound!



### **Mixture Approach**

PIF value now depends on truncation bound!



We propose two nonparametric methods: empirical method and approximate method

### **Methods - Empirical Method**

Let  $\hat{\mu}_n^{\text{obs}}(\boldsymbol{\beta}) = \frac{1}{n} \sum_{i=1}^n RR(\boldsymbol{X}_i; \boldsymbol{\beta}) \text{ and } \hat{\mu}_n^{\text{cft}}(\boldsymbol{\beta}) = \frac{1}{n} \sum_{i=1}^n RR(g(\boldsymbol{X}_i); \boldsymbol{\beta}).$ We define the empirical estimators of the PAF and PIF as:

$$\widehat{\mathsf{PAF}} := 1 - \frac{1}{\hat{\mu}_n^{\mathrm{obs}}(\hat{\boldsymbol{\beta}})}, \quad \text{and} \quad \widehat{\mathsf{PIF}} := 1 - \frac{\hat{\mu}_n^{\mathrm{cft}}(\hat{\boldsymbol{\beta}})}{\hat{\mu}_n^{\mathrm{obs}}(\hat{\boldsymbol{\beta}})}$$

### **Methods - Empirical Method**

Let  $\hat{\mu}_n^{\text{obs}}(\boldsymbol{\beta}) = \frac{1}{n} \sum_{i=1}^n RR(\boldsymbol{X}_i; \boldsymbol{\beta})$  and  $\hat{\mu}_n^{\text{cft}}(\boldsymbol{\beta}) = \frac{1}{n} \sum_{i=1}^n RR(g(\boldsymbol{X}_i); \boldsymbol{\beta})$ . We define the empirical estimators of the PAF and PIF as:

$$\widehat{\mathsf{PAF}} := 1 - \frac{1}{\hat{\mu}_n^{\mathrm{obs}}(\hat{\boldsymbol{\beta}})}, \quad \text{and} \quad \widehat{\mathsf{PIF}} := 1 - \frac{\hat{\mu}_n^{\mathrm{cft}}(\hat{\boldsymbol{\beta}})}{\hat{\mu}_n^{\mathrm{obs}}(\hat{\boldsymbol{\beta}})}$$

#### Theorem

Suppose that  $\hat{\beta}$  is a consistent and asymptotically normal estimator from an independent study. That is,  $\sqrt{m}(\hat{\beta} - \beta)$  is asymptotically mean-zero multivariate normal with covariance matrix  $\Sigma_{\beta}$ , where m is the sample size of the independent study estimating  $\beta$ . Then  $\widehat{PAF}$  and  $\widehat{PIF}$  converge in probability to PAF and PIF, respectively, and both  $\sqrt{n}(\widehat{PAF} - PAF)$ and  $\sqrt{n}(\widehat{PIF} - PIF)$  are asymptotically mean-zero multivariate normal.

Suppose we only had the mean  $\bar{\mathbf{X}} = (\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k)$  and variance  $\hat{\sigma}_{i,j} = Cov(X_i, X_j)$  of the exposure. This is often what is reported in publications, where *individual-level data is not available*.

Suppose we only had the mean  $\bar{\mathbf{X}} = (\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k)$  and variance  $\hat{\sigma}_{i,j} = Cov(X_i, X_j)$  of the exposure. This is often what is reported in publications, where *individual-level data is not available*.

We can use a second-order Taylor expansion for  $\hat{\mu}_n^{\text{obs}}(\hat{\beta})$  to derive a point estimate using *only the mean and variance*, leading to the following PAF estimator

$$\widehat{\mathsf{PAF}} = 1 - \frac{1}{RR(\bar{\boldsymbol{X}}; \hat{\boldsymbol{\beta}}) + \frac{1}{2}\sum_{i,j} \hat{\sigma}_{i,j} \frac{\partial^2 RR(\boldsymbol{X}, \hat{\boldsymbol{\beta}})}{\partial X_i \partial X_j}} \big|_{\boldsymbol{X} = \bar{\boldsymbol{X}}}$$

Suppose we only had the mean  $\bar{\mathbf{X}} = (\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k)$  and variance  $\hat{\sigma}_{i,j} = Cov(X_i, X_j)$  of the exposure. This is often what is reported in publications, where *individual-level data is not available*.

We can use a second-order Taylor expansion for  $\hat{\mu}_n^{\text{obs}}(\hat{\beta})$  to derive a point estimate using *only the mean and variance*, leading to the following PAF estimator

$$\widehat{\mathsf{PAF}} = 1 - \frac{1}{RR(\bar{\boldsymbol{X}}; \hat{\boldsymbol{\beta}}) + \frac{1}{2}\sum_{i,j} \hat{\sigma}_{i,j} \frac{\partial^2 RR(\boldsymbol{X}, \hat{\boldsymbol{\beta}})}{\partial X_i \partial X_j}} \big|_{\boldsymbol{X} = \bar{\boldsymbol{X}}}$$

Repeat for  $\hat{\mu}^{\text{cft}}(\hat{\beta})$  for the PIF.

Suppose we only had the mean  $\bar{\mathbf{X}} = (\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k)$  and variance  $\hat{\sigma}_{i,j} = Cov(X_i, X_j)$  of the exposure. This is often what is reported in publications, where *individual-level data is not available*.

We can use a second-order Taylor expansion for  $\hat{\mu}_n^{\text{obs}}(\hat{\beta})$  to derive a point estimate using *only the mean and variance*, leading to the following PAF estimator

$$\widehat{\mathsf{PAF}} = 1 - \frac{1}{RR(\bar{\boldsymbol{X}}; \hat{\boldsymbol{\beta}}) + \frac{1}{2}\sum_{i,j} \hat{\sigma}_{i,j} \frac{\partial^2 RR(\boldsymbol{X}, \hat{\boldsymbol{\beta}})}{\partial X_i \partial X_j}} \big|_{\boldsymbol{X} = \bar{\boldsymbol{X}}}$$

Repeat for  $\hat{\mu}^{\text{cft}}(\hat{\beta})$  for the PIF.

To derive the variance, we apply the multivariate delta method, as the PIF and PAF are functions of three components:  $\bar{\boldsymbol{X}}, \hat{\sigma}_{i,j}, \hat{\boldsymbol{\beta}}$ 

### **Simulation Studies**

- Define true exposure as a mixture p<sub>0</sub> + (1 p<sub>0</sub>)f(x), where f(x) is a known parametric distribution, truncated at M = 12. Get true PAF value.
- For each simulation  $b = 1, \ldots, B$ , varying N:
  - Generate data from true underlying exposure distribution
  - Estimate the PAF and 95% confidence interval using the approximate and empirical methods
- Report coverage and average relative bias over the B simulations

# **Simulation Studies**

True dist.	$p_0 + (1 - p_0)f(x)$			Empirical		Approximate	
f(x)	<i>P</i> 0	true PAF	N	Rel. Bias %	Coverage %	Rel. Bias %	Coverage %
Lognormal	0.00	0.364	100 1000				
	0.05	0.352	10000 100 1000				
	0.25	0.301	10000 100 1000				
	0.50	0.223	10000 100 1000				
	0.75	0.125	10000 100 1000				
Weibull	0.00	0.350	10000 100 1000				
	0.05	0.339	10000 100 1000				
	0.25	0.288	10000 100 1000				
	0.50	0.212	10000 100 1000				
	0.75	0.119	100 1000 10000				

# **Simulation Studies**

True dist.	$p_0 + (1 - p_0)f(x)$			Empirical		Approximate	
f(x)	<i>P</i> 0	true PAF	N	Rel. Bias %	Coverage %	Rel. Bias %	Coverage %
Lognormal	0.00	0.364	100	-25	81	-41	98
-			1000	-1	92	-15	94
			10000	0	94	-11	90
	0.05	0.352	100	-21	81	-39	97
			1000	0	92	-15	94
			10000	0	95	-12	89
	0.25	0.301	100	-29	79	-29	94
			1000	3	92	-15	93
			10000	0	95	-14	86
	0.50	0.223	100	22	77	-12	88
			1000	9	91	-15	92
			10000	1	95	-15	84
	0.75	0.125	100	23	77	15	84
			1000	17	91	-11	90
			10000	14	95	-14	86
Weibull 0.00	0.00	0.350	100	-30	86	-39	99
			1000	-3	94	-8	94
			10000	0	95	-4	95
	0.05	0.339	100	-26	86	-36	99
			1000	-2	94	-8	94
			10000	0	95	-5	94
	0.25	0.288	100	-11	84	-25	95
			1000	0	94	-8	94
			10000	0	95	-6	94
	0.50	0.212	100	17	83	-4	90
			1000	4	94	-7	93
			10000	1	95	-7	93
	0.75	0.119	100	60	83	28	85
			1000	10	93	-2	92
			10000	1	95	-5	94

- Q: What proportion of type 2 diabetes cases can be attributed to sugar-sweetened beverage consumption in Mexico?
- SSB consumption data (n = 7762) from ENSANUT 2016<sup>1</sup>
- Meta-analytic relative risk taken from the Mexican Teacher's Cohort<sup>2</sup>

<sup>&</sup>lt;sup>1</sup>Gaona-Pineda et al. 2018, <sup>2</sup>Stern et al. 2019

- Q: What proportion of type 2 diabetes cases can be attributed to sugar-sweetened beverage consumption in Mexico?
- SSB consumption data (n = 7762) from ENSANUT 2016<sup>1</sup>
- Meta-analytic relative risk taken from the Mexican Teacher's Cohort<sup>2</sup>



<sup>1</sup>Gaona-Pineda et al. 2018, <sup>2</sup>Stern et al. 2019

	Parameters	PAF (95% CI)
Standard Gamma	k=1.15,  heta=1.29	0.345
Mixture Gamma	$k = 1.41, \theta = 0.90$	0.280
Mixture Gamma ( $M=12$ )	k=1.41,  heta=0.90	0.290
Standard Lognormal	$\log\mu=0.082,\log\sigma=0.31$	1
Mixture Lognormal	$\log\mu=0.05,\log\sigma=0.98$	1
Mixture Lognormal ( $M = 12$ )	$\log\mu=0.05,\log\sigma=0.98$	0.379
Standard Normal	$\mu=1.48, \sigma=1.38$	0.278
Mixture Normal	$\mu=$ 1.56, $\sigma=$ 1.37	0.375
Mixture Normal ( $M = 12$ )	$\mu=1.56, \sigma=1.37$	0.375
Standard Weibull	$k=1.08, \lambda=1.53$	0.345
Mixture Weibull	$k=1.20, \lambda=1.66$	0.339
Mixture Weibull ( $M = 12$ )	$k=1.20, \lambda=1.66$	0.339
Empirical	-	0.345 (0.224, 0.467)
Approximate	-	0.325 (0.219, 0.431)

	Parameters	PAF (95% CI)
Standard Gamma	$k = 1.15, \theta = 1.29$	0.345
Mixture Gamma	k=1.41,  heta=0.90	0.280
Mixture Gamma ( $M = 12$ )	k=1.41,  heta=0.90	0.290
Standard Lognormal	$\log\mu=0.082,\log\sigma=0.31$	1
Mi×ture Lognormal	$\log\mu=0.05,\log\sigma=0.98$	1
Mixture Lognormal ( $M = 12$ )	$\log\mu=0.05,\log\sigma=0.98$	0.379
Standard Normal	$\mu=1.48,\sigma=1.38$	0.278
Mixture Normal	$\mu=$ 1.56, $\sigma=$ 1.37	0.375
Mixture Normal ( $M = 12$ )	$\mu=1.56,\sigma=1.37$	0.375
Standard Weibull	$k=1.08, \lambda=1.53$	0.345
Mixture Weibull	$k=1.20, \lambda=1.66$	0.339
Mixture Weibull ( $M = 12$ )	$k=1.20,\lambda=1.66$	0.339
Empirical	-	0.345 (0.224, 0.467)
Approximate	-	0.325 (0.219, 0.431)

pifpaf R package available at https://github.com/colleenchan/pifpaf

# Recap

- PIF estimation requires assuming some distribution for a continuous exposure
  - Biased when exposure distribution is misspecified and undefined when a heavy-tailed distribution is chosen
- We propose two nonparametric methods to estimate the PIF, both of which do not require making any distributional assumptions
  - Empirical method: Requires individual-level data
  - Approximate method: Requires only the mean and variance
- Conducted simulation studies of our methods
- PAF estimation of SSB consumption on type 2 diabetes incidence in Mexico ( $\approx 0.33$ )
- Possible extensions: nonparametric Bayesian inference, robust mean estimators for the PIF

# Thank you!

#### Email: colleen.chan@yale.edu

### The PIF and PAF as Causal Estimands

The PIF and PAF can interpreted as causal estimands if the following assumptions hold:

- $\beta$  is a causal parameter, i.e., the model used to estimate relative risk adjusts for all known confounders
- eta is transportable to the counterfactual population
- No effect modifiers

Consider a general function  $h(\mathbf{X})$ , which is twice differentiable. Let

$$\boldsymbol{D}h(\boldsymbol{X}) = rac{\partial h(\boldsymbol{X})}{\partial \boldsymbol{X}} \quad ext{and} \quad \boldsymbol{H}h(\boldsymbol{X}) = rac{\partial^2 h(\boldsymbol{X})}{\partial \boldsymbol{X} \partial \boldsymbol{X}^T}$$

The second-order Taylor polynomial for  $h(\mathbf{X})$  is

$$h(\mathbf{X}) \approx h(\widehat{\mu}) + \mathbf{D}h(\widehat{\mu})(\mathbf{X} - \widehat{\mu}) + \frac{1}{2}(\mathbf{X} - \widehat{\mu})^{\mathsf{T}}\mathbf{H}h(\widehat{\mu})(\mathbf{X} - \widehat{\mu})$$
  
=  $h(\widehat{\mu}) + \mathbf{D}h(\widehat{\mu})(\mathbf{X} - \widehat{\mu}) + \frac{1}{2}tr\left[(\mathbf{X} - \widehat{\mu})(\mathbf{X} - \widehat{\mu})^{\mathsf{T}}\mathbf{H}h(\widehat{\mu})\right]$ 

The first and second moments of  $\boldsymbol{X}$  are

$$\mu_{\boldsymbol{X}} = \mathbb{E}(\boldsymbol{X}) \quad ext{and} \quad \boldsymbol{\Sigma}_{\boldsymbol{X}} = Var(\boldsymbol{X}),$$

and their estimates are

$$\widehat{\boldsymbol{\mu}}_{\boldsymbol{X}} = \frac{1}{n} \sum_{i=1}^{n} (\boldsymbol{X}_{i}) \quad \text{and} \quad \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{X}} = \frac{1}{n} \sum_{i=1}^{n} (\boldsymbol{X}_{i} - \widehat{\boldsymbol{\mu}}_{\boldsymbol{X}}) (\boldsymbol{X}_{i} - \widehat{\boldsymbol{\mu}}_{\boldsymbol{X}})^{T}.$$

Applying the approximation to all subjects  $X_1, X_2, \ldots, X_n$ , we have

$$\frac{1}{n}\sum_{i=1}^{n}h(\boldsymbol{X}_{i})\approx h(\widehat{\boldsymbol{\mu}})+\frac{1}{2}tr\left[\widehat{\boldsymbol{\Sigma}}_{\boldsymbol{X}}\boldsymbol{H}h(\widehat{\boldsymbol{\mu}})\right].$$

Using this, we can approximate the following scalar functions,

$$\hat{\mu}_{n}^{\text{obs}}(\hat{\beta}), \hat{\mu}_{n}^{\text{cft}}(\hat{\beta}), \frac{1}{n} \sum_{i=1}^{n} (RR(X_{i}; \hat{\beta}))^{2}, \frac{1}{n} \sum_{i=1}^{n} (RR(g(X_{i}); \hat{\beta}))^{2}, \frac{1}{n} \sum_{i=1}^{n} RR(X_{i}; \hat{\beta}) RR(g(X_{i}); \hat{\beta}),$$

and the following vector functions, entry by entry,

$$\frac{1}{n}\sum_{i=1}^{n}\nabla_{\beta}RR(X_{i};\beta)\Big|_{\beta=\hat{\beta}} \text{ and } \frac{1}{n}\sum_{i=1}^{n}\nabla_{\beta}RR(g(X_{i});\beta)\Big|_{\beta=\hat{\beta}}$$

These calculations appear in the confidence intervals for  $\widehat{PAF}$  and  $\widehat{PIF}$ .

# pifpaf **R** package<sup>1</sup>

```
> x <- df$servina</pre>
> pif.ind(x, beta = log(1.27), varbeta = 0.002)
Estimating PAF and 95% confidence interval
$pif
[1] 0.3453349
$ci
[1] 0.2223366 0.4683332
> pif.app(meanx = 1.483, varx = 1.909, n = 7762, beta = log(1.27), varbeta = 0.002)
Estimating PAF and 95% confidence interval
$pif
[1] 0.3250859
$ci
F17 0.2184401 0.4317316
> pif.ind(x, beta = log(1.27), varbeta = 0.002, a = -1)
Estimating PIF with counterfactual exposure g(x) = x - 1 and 95% confidence interval
$pif
[1] 0.2036881
$ci
[1] 0.08078843 0.32658777
```

<sup>1</sup>https://github.com/colleenchan/pifpaf